

# Targetting Audits Using Predictive Analytics

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Exeter and IFS

July 2013

- The economic analysis of tax compliance has two objectives:
  - To explain and predict behaviour
  - To design beneficial interventions
- Different methodologies can contribute to this objective:
  - Theory
  - Empirical analysis
  - Experimentation
- This talk will focus on an additional methodology: *agent-based modelling*

- The talk begins with an introduction to agent-based modelling
- Successful application of agent-based modelling requires a credible model of individual compliance
- So the literature on modelling compliance is reviewed
- The talk is completed by reviewing my work with Nigar Hashimzade, Frank Page, and Matt Rablen
  - *Auditing rules*
  - *Predictive analytics*

- An agent-based model:
  - Creates a set of agents
  - Assigns abilities, objectives, and knowledge
  - Allows them to interact
  - Observes the outcome
- The creation and interaction takes place in a computer simulation
- Parameters can be varied to test the effect on the outcome
- Such models can describe natural situations or economic situations

# Sheep and Wolves

- A famous agent-based model of nature is that of sheep and wolves
- Wolves and sheep wander randomly around the landscape
- The wolves look for sheep to prey on
  - Each step costs wolves energy so they must eat sheep
  - When they run out of energy they die
- Sheep eat grass and reproduce
- The analysis simulates the evolution of the populations

- The same software can support a basic tax evasion model:
  - Apply the Allingham-Sandmo model of evasion choice
  - Adopt a random audit strategy
  - Track the degree of compliance
- Policy experiments permit the effect of interventions to be judged
- Provides a starting point for more detailed analysis

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<sup>1</sup>Thanks are due to Kim Bloomquist, IRS, for allowing use of the programme

- There are several limitations:
  - Most free software does not permit complex optimization
  - The implications of the preferences do not fit the facts
  - Interventions can be more sophisticated than random audits
- The first is solved through the use of alternative software (Matlab)
- The second motivates a review of the recent literature on compliance
- The analysis of sophisticated interventions is our current research question

- Our research focuses on modelling the *choice behaviour* behind the compliance decision
- We aim to integrate the best of current theory to match evidence
- The intention is to permit the exploration of policy interventions
- The models can use artificial data or be calibrated to actual data
- The next sections develop the components of the model



# Individual Compliance Behaviour

- Research on compliance behaviour has built on the basic model of Allingham-Sandmo (1972)
- The evasion level is chosen to maximize expected utility

$$\mathcal{E}U = pU(Y[1-t] - tE) + [1-p]U(Y[1-t] + tE)$$

- Where:
  - $p$  is the probability of audit
  - $Y$  is income
  - $t$  is the tax rate
  - $f$  is the fine levied on tax evaded
  - $E$  is the amount of evasion

- There are three basic problems with the predictions of this model
- *First*,  $E > 0$  if  $p < \frac{1}{1+F}$  which is satisfied for practical values ( $f$  is at most 2, so  $E > 0$  if  $p < 1/3$ )
- *Second*, decreasing absolute risk aversion is sufficient for  $\frac{dE}{dt} < 0$
- *Third*, the source of income also determines the *opportunity* for evasion:
  - Third-party reporting
  - Withholding
- Solutions proposed to improve the predictions include appeal to *non-expected utility theory* and to *social customs*

# Non-Expected Utility

- A general form of non-EU choice theory is

$$V = w_1(p, 1 - p)v(Y [1 - t] - tE) + w_2(p, 1 - p)v(Y [1 - t] + tE)$$

- Several alternatives have been proposed:
  - *Rank Dependent Expected Utility* imposes structure on the weighting functions
  - *Prospect Theory* uses weights, changes payoff functions, and comparison to a reference point
  - *Non-Additive Probabilities* do not require the normal consistency of aggregation for probabilities
  - *Ambiguity* permits uncertainty over the probability of outcomes
- The weighting functions (or *beliefs*) can improve predictions but still do not give  $\frac{dE}{dt} > 0$
- And these alternatives have their own shortcomings (Hashimzade, Myles and Tran-Nam, 2012)

- Yaniv (1999), al Nowaihi and Dhami (2001), and Bernasconi and Zanardi (2004) use variants of prospect theory
- Consider the standard Kahneman-Tversky value function

$$v(z) = \begin{cases} z^\beta, & \text{if } z > 0 \\ -\gamma(-z^\beta), & \gamma > 1, \text{ if } z < 0 \end{cases}$$

- And choose the reference point as the correct tax payment,  $Y[1 - t]$
- The payoff function becomes

$$V = E^\beta t^\beta [w_2 - w_1 \gamma f^\beta]$$

- So evasion is all or nothing (a consequence of the non-concave objective)

# Social Customs

- A social custom is an informal rule of behaviour that summarizes the *attitude* toward compliance
- A loss of utility is incurred if the custom is broken

$$V = \begin{cases} U(Y[1 - t]) + \chi^i, & \text{if } E = 0 \\ \mathcal{E}U, & \text{if } E > 0 \end{cases}$$

- There will be a cutoff  $\chi^*$  such that  $\chi^i < \chi^* \implies E > 0$  and  $\chi^i > \chi^* \implies E = 0$
- If  $\chi^i = \chi^i(m, E)$ , ( $m$  the proportion of population evading) evasion becomes a social decision
- Myles and Naylor (1996) show that  $\chi_m^i(m, E) < 0$  opens the possibility of multiple equilibria
- For some specifications it is also possible for  $\frac{dE}{dt} > 0$

# Attitudes, Beliefs, and Opportunities

- From these observations:
  - We do not need to feel bound by expected utility using objective probability
  - Similarly, there is no need to be restricted by any of the particular alternatives
- In short, we happily mix subjective beliefs with convenient functional forms
- Our model of the compliance decision combines *attitudes*, *beliefs*, and *opportunities* and recognizes the *social setting* for the decision
- Three uses of agent-based models are now described:
  - The effect of *opportunities* are considered within the Allingham-Sandmo framework
  - Next the endogenous development of *attitudes* and *beliefs* within a *social network* is added
  - The final step is to review the effect of *predictive analytics* on audit outcomes

- The model allows each individual to make a choice of occupation (a generalization of Pestieau and Posse, 1991)
- *Employment* is safe (wage is fixed) but tax cannot be evaded (withholding, third-party reporting)
- *Self-employment* is risky but provides an opportunity to evade
- An individual is described by  $\{w, \rho, s_1, s_2\}$  :
  - $w$  = wage in employment
  - $\rho$  = (relative) risk aversion
  - $s_i$  = skill in self-employment occupation  $i$

- The outcome of self-employment is  $s_i y_i$  where  $y_i$  is drawn from a lognormal distribution
- It is assumed that  $\mu(y_1) < \mu(y_2)$  and  $\sigma^2(y_1) < \sigma^2(y_2)$
- The evasion level is chosen after income from self-employment is known
- With outcome  $Y_i = s_i y_i$  the amount evaded  $E_i$  is determined by

$$\max E U_i = pU([1 - t] Y_i - ftE_i) + (1 - p)U([1 - t] Y_i + tE_i)$$

- The occupation offering highest (expected) utility is chosen

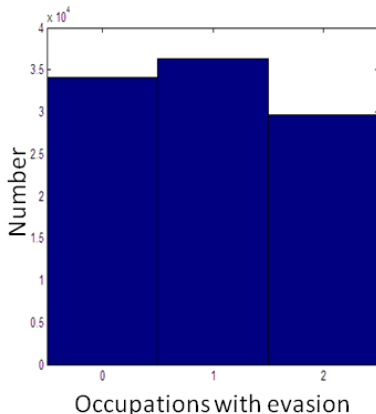
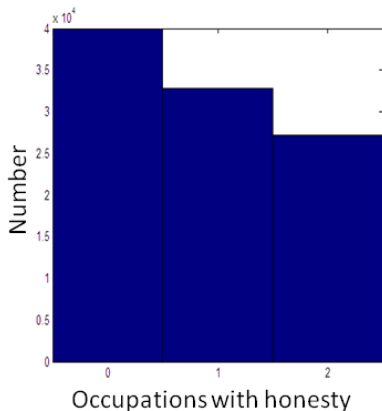


# Simulation Process

- Individual characteristics  $\{w, \rho, s_1, s_2\}$  are randomly drawn at the outset
- The simulation then iterates the following steps:
  - Occupation is chosen
  - Incomes are realized (as random draws in self-employment) and the evasion decision is made
  - The tax authority audits and punishes any evasion that is detected
- For each iteration the outcome with honesty and with evasion are calculated
- 1000 individuals in the simulation, 100 iterations and data averaged across iterations

# Evasion and Risk-Taking

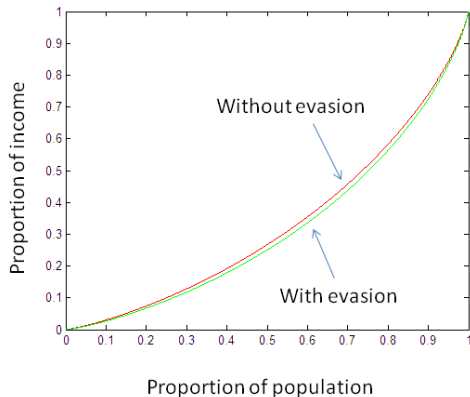
- The distribution of occupational choices shifts away from the safe occupation
- There is more occupational risk-taking when evasion is possible



# Evasion and Income Distribution

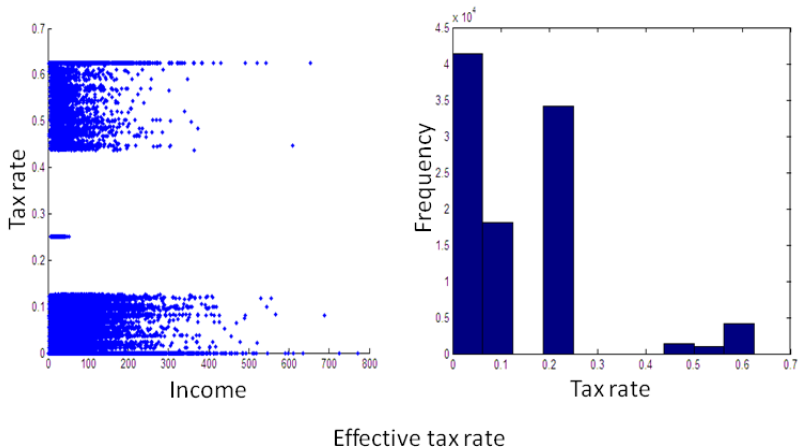
- Evasion increases mean income (after taxes and fines) and the inequality of income

	Honesty	Evasion
Mean Income	27.72	32.77
Gini Coefficient	0.464	0.492



# Evasion and the Effective Tax Rate

- The flat tax of 0.25 is undermined by evasion and punishments
- The distribution of effective tax rates is unrelated to income



- The analysis of tax evasion has demonstrated two important features:
  - The social setting influences the evasion decision (*attitudes*)
  - The probability of audit is subjective not objective (*beliefs*)
- We have incorporated these into the simulation by adding learning within a *social network*
- Individuals meet with their contacts in the network and meetings allow exchange of information on beliefs
- This can explain why social groups have different behaviour with respect to tax evasion

# Network and Meetings

- The network is described by a symmetric matrix  $A$  of 0s and 1s (bi-directional links)
- In each period a random selection of meetings occur described by a matrix  $C$  of zeros and ones
- Individuals  $i$  and  $j$  meet during a period if  $A_{ij}C_{ij} = 1$
- At a meeting of  $i$  and  $j$  there is a probability that information is exchanged
- The probability of information exchange depends on the occupational groups to which  $i$  and  $j$  belong
- The probabilities are given by  $p_{ij}$  where  $i, j = e, 1, 2$ , and  $p_{ii} > p_{ij}$ , all  $i, j, i \neq j$

# Audits and Belief Updating

- The belief about the probability of audit is determined by audits and interaction
- Occupational choice in period  $t$  is made on the basis of the belief  $p_t^i$
- The updating effect of an audit is

$$\tilde{p}_t^i = X_t^i P + (1 - X_t^i) d(p_t^i), \quad P \in [0, 1]$$

where  $X_t^i = 1$  if  $i$  was audited in  $t$  and  $X_t^i = 0$  otherwise

- Two different processes for the formation of subjective beliefs:
  - *Target effect*:  $P = 1$  and  $d(p_t^i) = \delta p_t^i$ ,  $\delta \in [0, 1]$  (rise, then decay)
  - *Bomb-crater effect* (Guala and Mittone, 2005):  $P = 0$  and  $d(p_t^i) = p_t^i + \delta(1 - p_t^i)$ ,  $\delta \in [0, 1]$  (fall, then rise)
- The evidence on which is correct is not compelling

- Individuals meet *after* audits take place
- *If an information exchange occurs* at a meeting the belief is updated according to the rule

$$p_{t+1}^i = \mu \tilde{p}_t^i + (1 - \mu) \left[ X_t^j P + (1 - X_t^j) \tilde{p}_t^j \right]$$

- This can also be written

$$p_{t+1}^j = \begin{cases} \mu \tilde{p}_t^i + (1 - \mu) P, & \text{if } j \text{ audited at } t \\ \mu \tilde{p}_t^i + (1 - \mu) \tilde{p}_t^j, & \text{otherwise} \end{cases}$$

- The belief  $p_{t+1}^i$  is carried into the next period



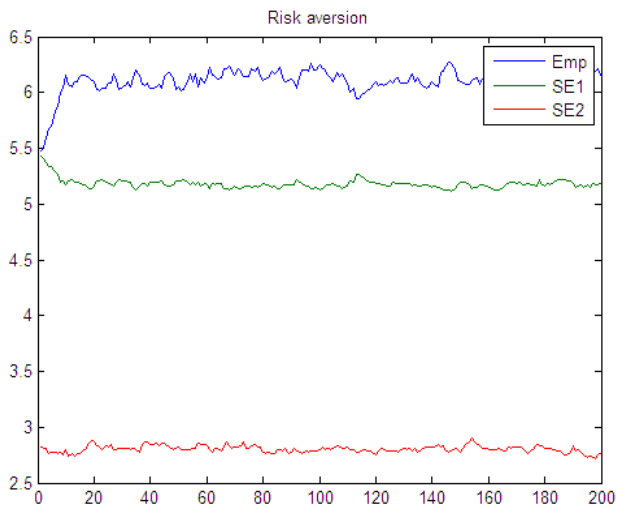
- The importance of the social custom is determined by interaction in the social network
- Each individual is randomly assigned a level of importance,  $\chi_0^i$ , at time 0
- This value is then updated each period *if* there is an information exchange between two individuals
- The updating process is described by

$$\chi_{t+1}^i = \frac{1}{X(i) + 1} \left[ \chi_t^i X(i) + \mathbf{1}_{[E_t^j=0]} \right]$$

where  $X(i)$  is the number of previous meetings for  $i$  at which information was exchanged

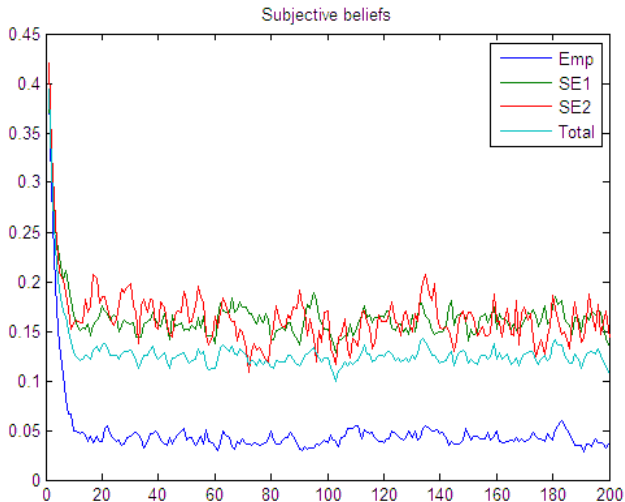
- $\chi_{t+1}^i > \chi_t^i$  if information is exchanged with an honest taxpayer and  
 $\chi_{t+1}^i < \chi_t^i$  if information is exchanged with an evader

# Risk Aversion

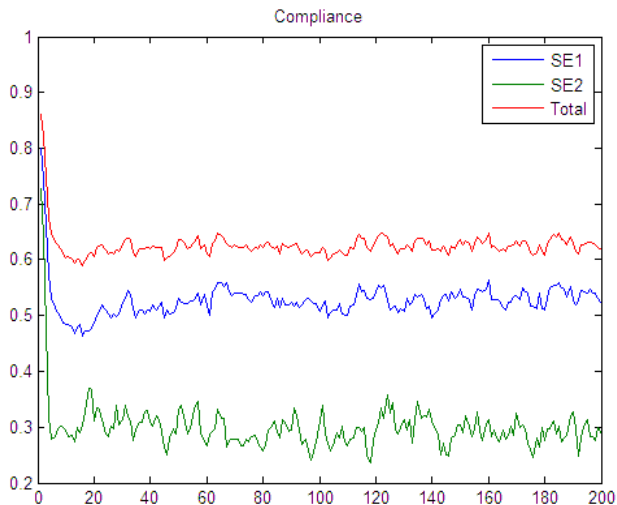


# Subjective Beliefs

Audit probability = 0.05



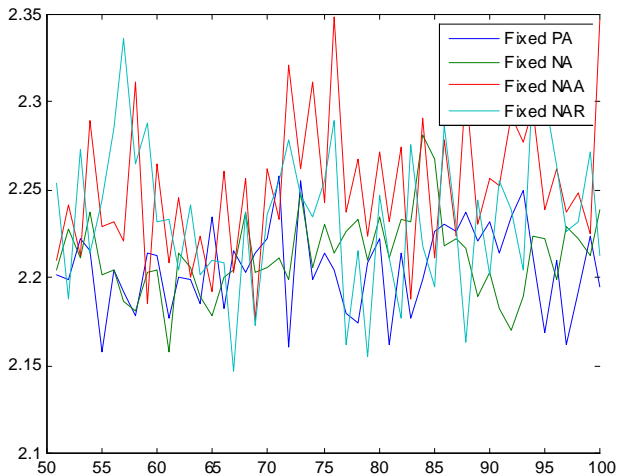
# Compliance



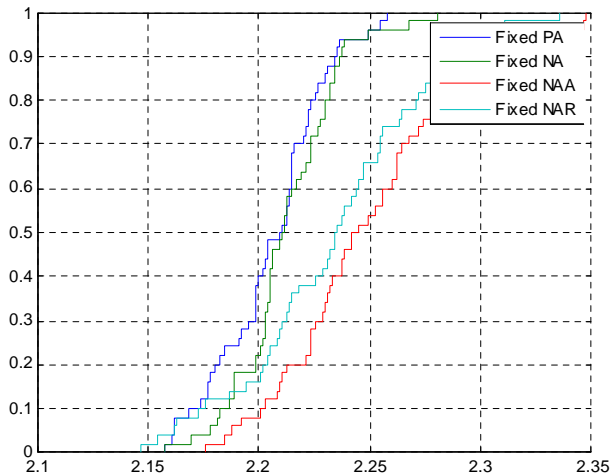
- The model is sufficiently rich to permit a range of questions to be investigated
- We have considered
  - The optimal number of random audits
  - Alternative audit strategies
  - The choice between audit types (hard or soft)
- The focus here will be on alternative audit strategies

- Four audit strategies are analyzed:
  - FixedPA: Random audit of the self-employed with a fixed probability
  - FixedNA: Audit a fixed number of taxpayers in each occupation
  - FixedNAA: Switches audits between occupations each period
  - FixedNAR: Randomly switches audits between occupations
- The fixed numbers match the expected number from the random audit

## Tax and Fine Revenues



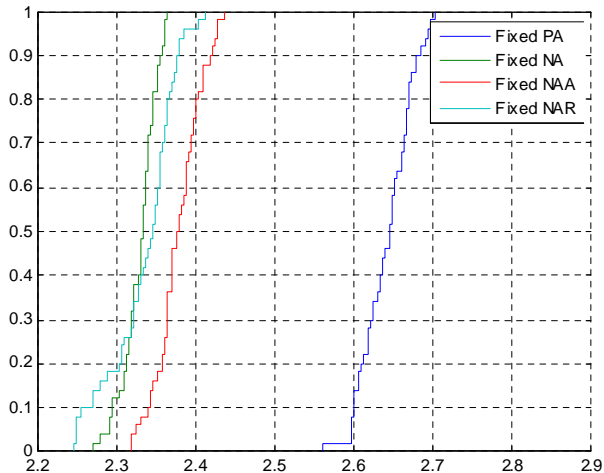
## Empirical CDFs





- An extension to the model is to allow each taxpayer to have separate beliefs about the audit probability in the two occupations
- Beliefs are now the pair  $\{p_t^i(1), p_t^i(2)\}$
- If the taxpayer works in occupation  $j$  then  $p_t^i(j)$  adjusts as before
- In contrast  $p_t^i(j')$  only adjusts if information is exchanged with someone working in occupation  $j'$

## Empirical CDFs

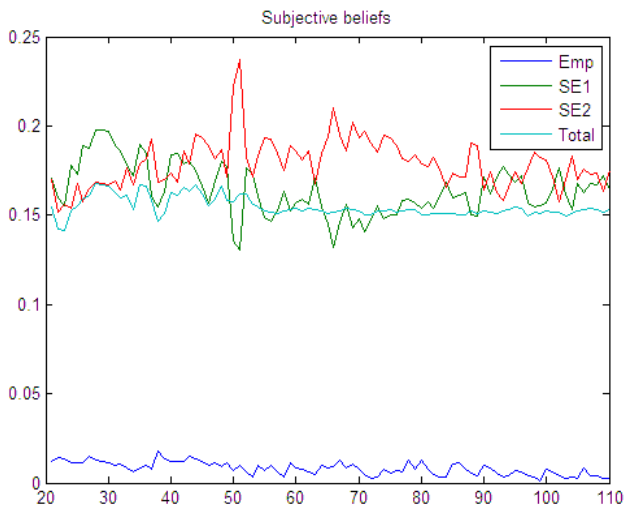


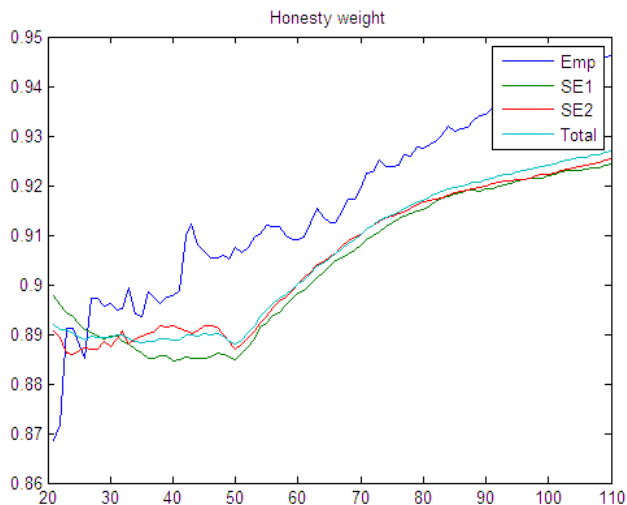
- The role of *predictive analytics* is to identify the best audit targets
- Predictive analytics are used by the IRS, HMRC etc.
- Various methods are used including credit scoring and econometric analysis
- We want to explore the effects of predictive analytics and whether they can improve on the other audit strategies
- The analysis compares the outcome of predictive analytics based on tax return data with that of random audits

- The simulation uses random audits for the first 50 periods
- The data from audits is collected and used to run a Tobit (censored) regression
- The amount of non-compliance is regressed on *occupation*, *declaration*, and *audit history*
- The estimated equation is used to predict non-compliance
- For periods 51-80 the top 5 percent are audited and audit outcomes used to update regression
- For periods 81-110 the top 2.5 percent are audited and 2.5 percent are randomly audited

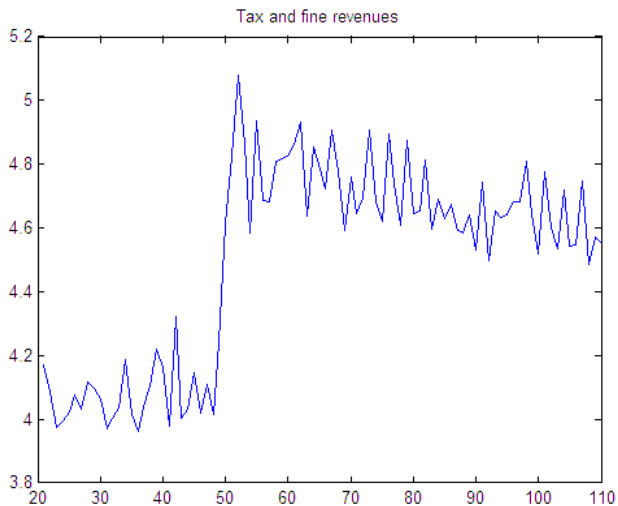
# Predictive Analytics





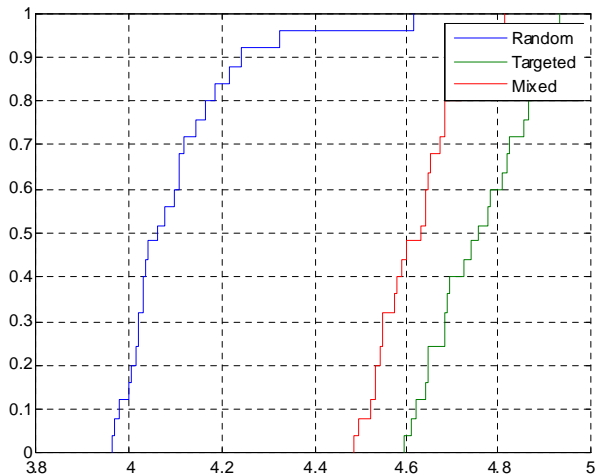


# Predictive Analytics





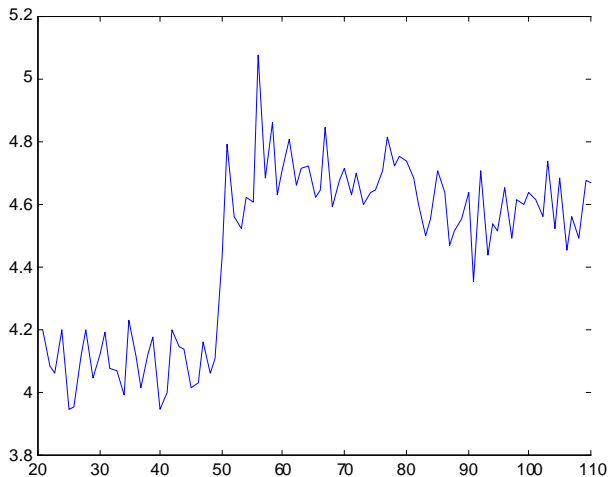
# Predictive Analytics



- The results show clearly that the use of predictive analytics increase tax and fine revenue
- Underlying this is an increase in the honesty weight when the predictive analytics operate
- Compliance is not uniformly increased in occupational groups if there is some randomness
- Extending to the dual probabilities does not affect the conclusion

# Predictive Analytics with Dual Probabilities

## Tax Revenues



- Agent-based modelling is a useful tool for testing policies
- The modelling can incorporate recent advances in the theory of compliance
- Our work emphasizes the role of attitudes, beliefs, and opportunities
- Compliance behaviour can vary significantly across occupational groups
- Predictive analytics is successful in encouraging compliance and increasing revenue